

# NAVAL POSTGRADUATE SCHOOL Monterey, California

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# **THESIS**

THERMOELECTRIC COOLER DESIGN

by

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December 1992

Thesis Advisor:

Allan D. Kraus

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# Thermoelectric Cooler Design

by

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Submitted in partial fulfillment of the requirements for the degree of

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#### **ABSTRACT**

Thermoelectric Cooler Design is a Microsoft Windows program to be used as an aid in the design of thermoelectric cooler devices. This program was written to be used to quickly model and compare alternative designs. A couple's optimum coefficient of performance and maximum heat pumping can be quickly determined. Other major features of the program include the ability to change material properties and dimensions of couples, analyze cascaded couples, and graph performance parameters. A brief description of thermoelectric cooler theory, modelling assumptions and complete source code listing is included.

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#### I. INTRODUCTION

#### A. FEATURES OF THERMOELECTRIC COOLERS

The unique features of thermoelectric coolers include:

- 1. Compact.
- 2. No moving parts.
- 3. The coefficient of performance is independent of capacity.
- 4. The cooling rate is easily controlled.
- 5. Reversible operation is possible allowing heating as well as cooling.
- 6. Vibration-free operation.
- 7. Precise temperature control.

#### **B. SPACEBORNE APPLICATIONS**

Thermoelectric coolers offer an alternative solution to cooling and heating requirements of spacecraft. Spaceborne applications for thermoelectric coolers include:

1. Equipment cooling -- removal of waste heat in order to maintain components at their optimal operating temperature. Thermoelectric coolers are especially useful for the control of small hot spots.

- 2. Life support temperature control -- thermoelectric coolers are very reliable making them ideally suited for long duration missions such as the space station or manned Mars mission.
- Cooling of infrared detectors -- thermoelectric coolers eliminate the need for coolant and associated support equipment. Of even more importance is the elimination of consumable coolants which also increases the life of the spacecraft.
- 4. Microgravity applications -- thermoelectric coolers offer precise, vibration-free temperature control for free-flying orbiting microgravity research platforms.

Reliability, the lack of moving parts or consumables, and vibration-free operation are especially important to spaceborne cooling systems.

# II. THERMOELECTRIC COOLER THEORY

# A. THERMOELECTRIC COUPLE CONFIGURATION

In it's most basic form, a thermoelectric couple consists of two dissimilar elements with contact at two junctions. Figure 1 shows a simple thermoelectric circuit consisting of two elements, physically joined on one side while electrically joined at the other.

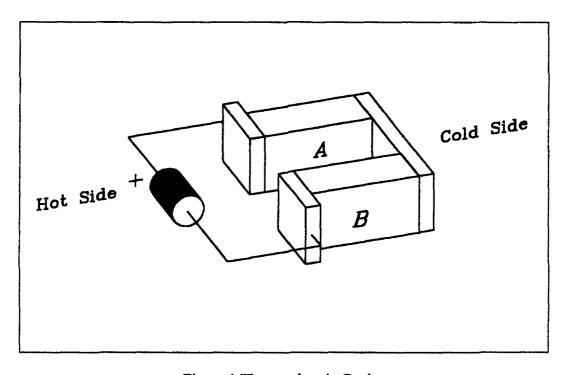


Figure 1 Thermoelectric Cooler

#### B. THERMOELECTRIC EFFECTS

The background for this section was gathered from Kraus [Ref. 12:pp. 294-303] and Ioffe [Ref. 2:pp. 96-128]. Three thermoelectric effects are known; the Seebeck, Peltier, and Thomson effects.

#### 1. Seebeck Effect

Consider the junction of two materials, A and B. If a temperature differential exists between the two junctions, one junction may be referred to as the hot side and the other the cold side. An open circuit voltage can be measured between the two junctions. This net conversion of thermal energy into electrical energy under zero current conditions is known as the Seebeck effect. The voltage observed, referred to as the Seebeck voltage, is proportional to the temperature differential between the hot and cold sides of the couple:

$$dE_S \propto dT$$

$$dE_S = \pm \alpha dT$$

$$E_S = \pm \int_{T_1}^{T_2} \alpha dT \quad (V) \tag{1}$$

where

 $E_S$  = Seebeck voltage (V)

 $\alpha$  = Seebeck coefficient of material (V/°C)

In the case of the couple composed of materials A and B,

$$\alpha = |\alpha_A| + |\alpha_B|$$

where

 $\alpha_A$  = Seebeck coefficient of material A  $\alpha_B$  = Seebeck coefficient of material B

#### 2. Peltier Effect

The Peltier effect is localized at the junctions between materials A and B. When a current flows through the junction, heat is either generated or absorbed depending on the direction of the current flow. The amount of heat is proportional to the current and is known as the Peltier heat:

$$dQ_D \propto Idt$$

$$dQ_{\mathcal{D}} = \pm \pi I dt$$

$$q_p = \pm \pi I \quad (W) \tag{2}$$

where

Qp = Peltier heat (J) qp = Peltier heat flow (W) I = Current (A)  $\pi$  = Peltier coefficient of material (V)

#### 3. Thomson Effect

This effect concerns the absorption or generation of heat in a conductor carrying a current in the presence of a temperature gradient. The amount of heat is proportional to the current and temperature gradient:

$$dQ_t \propto I dT dt$$

$$dQ_t = \pm \sigma I \, dT dt$$

$$dq_t = \pm \sigma I dT$$

$$q_t = \pm \sigma I \int_{T_1}^{T_2} dT \quad (W)$$
 (3)

where

 $Q_t = \text{Thomson heat } (J)$ 

 $q_t = \text{Thomson heat (W)}$ 

I = Current(A)

 $\sigma$  = Thomson coefficient of material (V/°C)

Because the product of  $\sigma$  and  $\Delta T$  is a voltage, the Thomson voltage is therefore:

$$E_t = \pm \int_{T_1}^{T_2} \sigma dT \quad (V) \tag{4}$$

#### C. IRREVERSIBLE EFFECTS

#### 1. Joule Effect

The evolution of heat when a current passes through a material may be referred to as the Joule heat flow:

$$q_i = I^2 R \quad (W) \tag{5}$$

In the case of a couple, the elements A and B are connected in electrical series regardless of the direction of the current flow:

$$R = \frac{\rho_A L_A}{A_A} + \frac{\rho_B L_B}{A_B} \quad (\Omega)$$
 (6)

where

 $\rho_A$ ,  $\rho_B$  = electrical resistivity of materials A and B ( $\Omega$  cm)

 $L_A$ ,  $L_B$  = Length of materials A and B (cm)

 $A_A$ ,  $A_B$  = Cross sectional area of materials A and B (cm<sup>2</sup>)

#### 2. Fourier Effect

The conduction of heat through a material is given by:

$$q_f = \left(\frac{KA}{L}\right) \Delta T \quad (W) \tag{7}$$

and, in the case of a couple with the elements in thermal parallel,

$$K = \frac{k_A A_A}{L_A} + \frac{k_B A_B}{L_B} \quad (W/^{\circ}C)$$
 (8)

where

 $k_A$ ,  $k_B$  = Thermal conductivity of materials A and B (W/cm $^{\circ}$ C)

 $L_A$ ,  $L_B$  = Length of materials A and B (cm)

 $A_A$ ,  $A_B$  = Cross sectional area of materials A and B (cm<sup>2</sup>)

#### D. NET HEAT ABSORBED AT COLD JUNCTION OF COUPLE

In this analysis, the Thomson heat will be neglected which greatly simplifies couple design procedure without any significant error Kraus [Ref. 1:p. 300] and Cadoff [Ref. 3:p. 8]. To determine the net heat pumped by the couple, the temperature distribution along the elements of the couple must be determined. Consider a single thermoelectric element as indicated in Figure 2, where  $A_X$  is the cross sectional area of the element normal to the flow of current and heat.

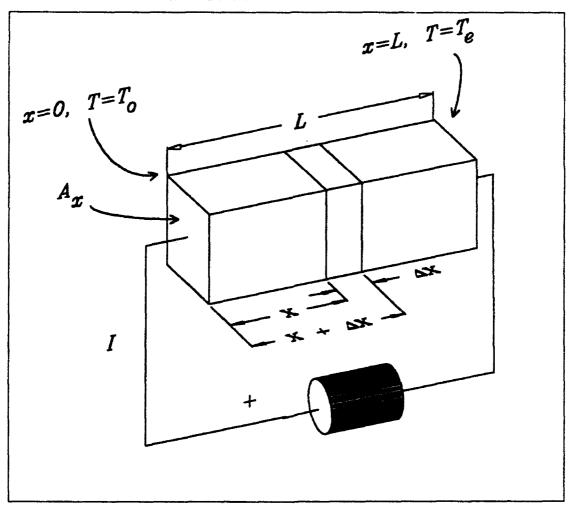


Figure 2 Thermoelectric Element

Here, the boundary conditions are:

$$T = T_O$$
 at  $x = 0$   
 $T = T_C$  at  $x = L$ 

Assuming steady state temperature conditions, there are three heat quantities which pertain to an energy balance over the incremental length,  $\Delta x$ :

1. The Fourier heat entering at point x:

$$q_X = -kA_X \left[ \frac{dT}{dx} \right]_X$$

2. The Joulean heat generated in the increment  $\Delta x$ :

$$q_j = \frac{I^2 \rho \Delta x}{Ax}$$

3. The Fourier heat leaving at point  $x + \Delta x$ :

$$q_{x+\Delta x} = -k A_x \left[ \frac{dT}{dx} \right]_{x+\Delta x}$$

The energy balance in the steady state requires that the heat leaving must be equal to the sum of the heat entering and the heat generated in the increment  $\Delta x$ :

$$qx + q_j = q_{x+\Delta x}$$

Substituting for  $q_x$ ,  $q_{x+\Delta x}$  and  $q_j$  gives

$$-kA_{x}\left[\frac{dT}{dx}\right]_{x} + \frac{I^{2} \rho \Delta x}{A_{x}} = -kA_{x}\left[\frac{dT}{dx}\right]_{x+\Delta x}$$

or with some algebra,

$$kA_x\left(\left[\frac{dT}{dx}\right]_{x+\Delta x} - \left[\frac{dT}{dx}\right]_x\right) + \frac{I^2 \rho \Delta x}{A_x} = 0$$

Dividing through by  $\Delta x$  yields

$$kA_{x}\left(\frac{\left[\frac{dT}{dx}\right]_{x+\Delta x}-\left[\frac{dT}{dx}\right]_{x}}{\Delta x}\right)+\frac{I^{2}\rho}{A_{x}}=0$$

And taking the limit as  $\Delta x \rightarrow 0$  gives

$$\lim_{x \to 0} \left[ kA_x \left( \frac{\left[ \frac{dT}{dx} \right]_{x + \Delta x} - \left[ \frac{dT}{dx} \right]_x}{\Delta x} \right) + \frac{I^2 \rho}{A_x} \right] = 0$$

which can be adjusted to

$$kAx \frac{d^2T}{dx^2} + \frac{I^2\rho}{Ax} = 0 ag{9}$$

The general solution to this simple differential equation is obtained through the use of a double integration:

$$\frac{d^2T}{dx^2} + \frac{I^2 \rho x}{kA_r^2} + C_1 = 0$$

and

$$T + \frac{I^2 \rho x^2}{2kA_x^2} + C_1 x + C_2 = 0$$

Applying the boundary conditions for the hot side where x = 0 and  $T = T_0$ :

$$C_2 = -T_0$$

and

$$T - T_0 + \frac{I^2 \rho x^2}{2kA_x^2} + C_1 x = 0$$

At the cold side of the element where x = L and  $T = T_e$ :

$$T_e - T_o + \frac{I^2 \rho L^2}{2kA_r^2} + C_1 L = 0$$

The solution for C<sub>1</sub>, the first constant of integration, is seen to be

$$C_1 = \frac{T_0 - T_e}{L} - \frac{I^2 \rho L}{2kA_x^2}$$

so that the particular solution of this simple, second order, differential equation which gives the temperature profile as a function of distance along the element:

$$T - T_0 + \frac{I^2 \rho x^2}{2kA_x^2} + \left(\frac{T_0 - T_e}{L}\right) x - \left(\frac{I^2 \rho L}{2kA_x^2}\right) x = 0$$

OT

$$T(x) = -\left(\frac{I^2 \rho}{2kA_x^2}\right) x^2 - \left(\frac{T_O - T_e}{L} - \frac{I^2 \rho L}{2kA_x^2}\right) x + T_O$$
 (10)

which is seen to be parabolic.

Figure 3 illustrates a temperature distribution for a typical element with the following parameters:

$$z = 3.08 \times 10^{-3} \text{ (°C}^{-1})$$

$$R = 1.73 \times 10^{-3} \text{ (}\Omega\text{)}$$

$$K = 3.64 \times 10^{-2} \text{ (}W/^{\circ}\text{C}\text{)}$$

$$\alpha = 4.4 \times 10^{-4} \text{ (}V/^{\circ}\text{C}\text{)}$$

$$\Delta T = 50 \text{ °C}$$
(11)
(12)
(13)
(14)
(15)

Due to the parabolic temperature distribution, the Joulean heat will be transferred to both the cold and hot junctions of the couple.

Differentiating equation (10), setting the derivative equal to zero,

$$\frac{dT}{dx} = -\frac{I^2 \rho X}{kA_x^2} - \frac{T_0 - T_e}{L} + \frac{I^2 \rho L}{2kA_x^2} = 0$$

permits a solution for x = X which is the position where the maximum temperature occurs:

$$X = \frac{\frac{I^2 \rho L}{2kA_x^2} - \frac{T_0 - T_e}{L}}{\frac{I^2 \rho X}{kA_x^2}}$$

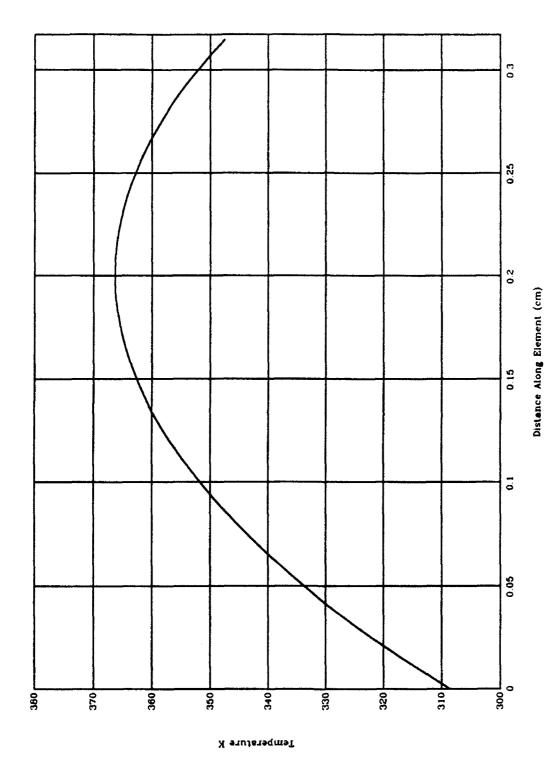


Figure 3 Temperature Profile Along Element

Rearranging and substituting  $\Delta T$  for  $T_0 - T_e$ :

$$X = \frac{L}{2} - \frac{k \Delta T A_x^2}{I^2 \rho L}$$

Assuming x = L and defining f as the fraction of the Joulean heat transferred to the cold junction:

$$f = \frac{L - X}{L} = \frac{1}{2} + \frac{k \Delta T A_x^2}{I^2 \rho L^2}$$

or

$$f = \frac{1}{2} + \frac{K\Delta T}{I^2 R} \tag{17}$$

where K and R are defined by equations (6) and (8), respectively.

The net heat absorbed at the cold junction of the couple is equal to the summation of the Peltier heat, minus the fraction of Joulean heat transferred to the cold junction:

$$q_{net} = \alpha I T_C - f I^2 R$$

and upon substitution of the expression for f given by equation (17):

$$q_{net} = \alpha I T_C - \frac{1}{2} I^2 R - K \Delta T \quad (W)$$
 (18)

Therefore the net heat pumped is the Peltier heat developed at the cold junction less the sum of one half the Joulean heat produced in the couples and the heat due to conduction from the hot junction to the cold junction.

# III. THERMOELECTRIC COOLER MODEL

#### A. INTRODUCTION

The equations in this chapter were used to model the thermoelectric cooler couple operating parameters and were given by Kraus [Ref. 1:pp. 303 - 326].

#### **B. HEAT PUMPING**

# 1. Current Yielding Maximum Heat Pumped

The equation for net heat pumped

$$q_{net} = \alpha I T_C - \frac{1}{2} I^2 R - K \Delta T \quad (W)$$
 (18)

may be differentiated with respect to current, *I*. When the derivative is set equal to zero, the current that yields maximum heat pumped is obtained:

$$\frac{dq}{dI} = \alpha T_C - IR = 0$$

Solving for I:

$$I_{m} = \frac{\alpha T_{C}}{R} \quad (A)$$

#### 2. Maximum Heat Pumped

Substituting  $I_m$  into the equation for the net heat pumped yields the maximum heat pumped:

$$q_m = \frac{\alpha^2 T_c^2}{2R} - K\Delta T \quad (W)$$
 (20)

# C. MAXIMUM TEMPERATURE DIFFERENTIAL

Heat pumped as a function of current is shown in Figure 4 using the parameters defined in equations (11) through (16). Setting equation (20) which is the maximum heat pumped equal to zero and solving for  $\Delta T$ , one obtains the maximum temperature differential between the hot and cold sides of the couple:

$$\Delta T_m = \frac{\alpha^2 T_C^2}{2KR} \quad (K)$$
 (21)

#### D. OPTIMUM RATIO OF ELEMENT CROSS SECTIONAL AREAS

The maximum temperature differential given by equation (21), can be increased by minimizing the product KR from equations (6) and (8):

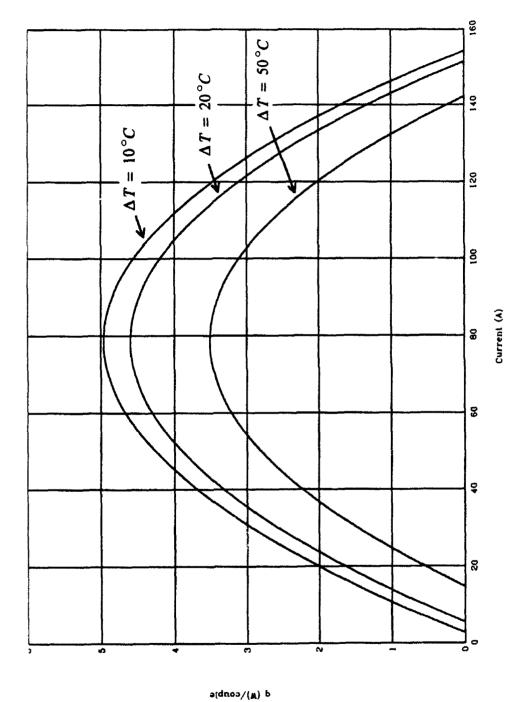


Figure 4 Heat Pumped as a Function of Current

$$KR = \left(\frac{\rho_A L_A}{A_A} + \frac{\rho_B L_B}{A_B}\right) \left(\frac{k_A A_A}{L_A} + \frac{k_B A_B}{L_B}\right) \tag{22}$$

and if  $L_A = L_B$  an expansion gives

$$KR = k_A \rho_A + k_B \rho_A \frac{A_B}{A_A} + k_A \rho_B \frac{A_A}{A_B} + k_B \rho_B$$
 (23)

An optimization of equation (23) can be accomplished by finding the point where the derivative with respect to the area ratio,  $A_A/A_B$ , vanishes:

$$\frac{dKR}{d(A_A/A_B)} = k_A \rho_B - k_B \rho_A \left(\frac{A_B}{A_B}\right)^2 = 0$$
 (24)

Then, a solution of equation (24) yields the area ratio that minimizes KR. Thus, in turn yields the optimal  $\Delta T_m$ :

$$\frac{A_A}{A_B} = \sqrt{\frac{\rho_A k_B}{\rho_B k_A}} \tag{25}$$

The area ratio given by equation (25) when substituted into equation (22), yields the optimum value of KR, designated by  $\phi$ 

$$\phi = k_A \rho_A + 2 \sqrt{k_A \rho_A k_B \rho_B} + k_B \rho_B$$

or

$$\phi = \left(\sqrt{k_A \rho_A} + \sqrt{k_B \rho_B}\right)^2 \tag{26}$$

Equation (16) has the restrictions that  $L_A = L_B$  and that the area ratio be determined using equation (25).

### E. FIGURE OF MERIT OF ELEMENT MATERIALS

Substituting  $\phi$ , equation (26), into the equation for  $\Delta T_m$  equation (21):

$$\Delta T_m = \frac{\alpha^2}{2\phi} T_c^2$$

or

$$\Delta T_m = \frac{1}{2} z T_c^2$$

where z, the figure of merit of the materials, is defined as:

$$z \equiv \frac{\alpha^2}{\phi}$$

which may be rewritten as:

$$z = \frac{\alpha^2}{\left(\sqrt{k_A \rho_A} + \sqrt{k_B \rho_B}\right)^2}$$

When  $L_A = L_B$  and the area ratio determined from equation (25), the figure of merit is a function of the properties of the elements. To maximize the figure of merit, the materials used should have a high Seebeck coefficient, low thermal conductivity, and low electrical resistivity Cadoff [Ref. 3: p. 21].

# F. POWER REQUIRED TO OPERATE THE COUPLE

To operate the couple, a voltage equal to the sum of the Seebeck voltages in the couple and the resistive voltage drop must be applied Kraus [Ref. 1: p. 304]. The power required to operate the couple is then:

$$P = IV = I(\alpha \Delta T + IR) \quad (W)$$
 (27)

#### G. COEFFICIENT OF PERFORMANCE

The coefficient of performance, $\eta$ , measures the performance of the couple and is the heat pumped, q, divided by the power required to operate the couple, P:

$$\eta = \frac{q}{P} \tag{28}$$

Substituting equation (18) for q and equation (27) for P gives

$$\eta = \frac{\alpha I T_C - \frac{1}{2} I^2 R - K \Delta T}{I(IR + \alpha \Delta T)}$$
 (29)

#### 1. Coefficient Of Performance At Maximum Heat Pumping

One may express  $q_m$  in terms of  $\Delta T$  and  $\Delta T_m$  using equations (20) and (21):

$$q_{m} = \frac{\alpha^{2} T_{C}^{2}}{2R} - K\Delta T = \frac{K\alpha^{2} T_{C}^{2}}{2KR} - K\Delta T$$

$$q_{m} = K\Delta T_{m} - K\Delta T = K(\Delta T_{m} - \Delta T)$$

$$q_{m} = K\Delta T_{m} \left(1 - \frac{\Delta T}{\Delta T_{m}}\right)$$
(30)

In similar fashion,  $P_m$  may be expressed in terms of the temperatures by substituting equation (19) into equation (27):

$$P_{m} = \alpha I_{m} \Delta T + I_{m}^{2} R$$

$$= \frac{\alpha^{2} T_{c} \Delta T}{R} + \frac{\alpha^{2} T_{c}^{2}}{R}$$

$$= \frac{\alpha^{2} T_{c}^{2}}{R} \left( \frac{\Delta T}{T_{c}} + 1 \right)$$

$$= \frac{2K\alpha^{2} T_{c}^{2}}{2KR} \left( 1 + \frac{\Delta T}{T_{c}} \right)$$

$$= 2K\Delta T_{m} \left( 1 + \frac{\Delta T}{T_{c}} \right)$$
(31)

To obtain the coefficient of performance when the couple is adjusted for maximum heat pumping, substitute equations (30) and (31) into equation (28) for the coefficient of performance:

$$\eta_{m} = \frac{q_{m}}{P_{m}} = \frac{K\Delta T_{m} (1 - \Delta T/\Delta T_{m})}{2 K\Delta T_{m} (1 + \Delta T/\Delta T_{c})}$$

$$\eta_{m} = \frac{1 - \Delta T/\Delta T_{m}}{2 (1 + \Delta T/\Delta T_{c})}$$

#### 2. Current Yielding Optimum Coefficient Of Performance

The expression for the coefficient of performance, equation (29),

$$\eta = \frac{\alpha I T_C - \frac{1}{2} I^2 R - K \Delta T}{I(IR + \alpha \Delta T)}$$

may be differentiated to find the current that yields the maximum coefficient of performance. This current is the value of I that causes  $d\eta/dI$  to vanish:

$$\frac{d\eta}{dI} = \frac{I(IR + \alpha\Delta T)(\alpha T_C - IR) - (\alpha I T_C - I^2 R/2 - K\Delta T)(2IR + \alpha\Delta T)}{I^2(IR + \alpha\Delta T)^2} = 0$$

OF

$$(I^2R + \alpha I\Delta T)(\alpha T_C - IR) = (\alpha IT_C - I^2R/2 - K\Delta T)(2IR + \alpha \Delta T)$$

Expansion gives:

$$I^{2}R\alpha T_{C} - I^{3}R^{2} + \alpha^{2}IT_{C}\Delta T - \alpha I^{2}R\Delta T = 2I^{2}R\alpha T_{C} + \alpha^{2}IT_{C}\Delta T$$
$$-I^{3}R^{2} - \alpha I^{2}R\Delta T/2 - 2IRK\Delta T - \alpha K\Delta T^{2}$$

or

$$\alpha I^2 R \Delta T/2 + \alpha T_C I^2 R - 2 K I R \Delta T - K \alpha \Delta T^2 = 0$$

which is actually a quadratic in I:

$$R\alpha\left(\frac{\Delta T}{2} + T_C\right)I^2 - (2KR\Delta T)I - \left(K\alpha\Delta T^2\right) = 0$$

which possesses a solution

$$I = \frac{2KR\Delta T \pm \sqrt{(2KR\Delta T)^2 + 4KR\alpha^2\Delta T^2[(\Delta T/2) + T_C]}}{2R\alpha[(\Delta T/2) + T_C]}$$
(32)

The value of the radical in equation (32) will always be greater than  $2KR\Delta T$  because it contains the sum of  $(2KR\Delta T)^2$  and another, positive term. For cooling to occur, the current must not be negative so the solution in which the radical term is subtracted is ignored:

$$I = \frac{2KR\Delta T + \sqrt{(2KR\Delta T)^2 + 4KR\alpha^2\Delta T^2[(\Delta T/2) + T_C]}}{2R\alpha[(\Delta T/2) + T_C]}$$

factoring  $4(KR)^2 \Delta T^2$  from under the radical gives:

$$I = \frac{2KR\Delta T + 2KR\Delta T\sqrt{1 + (\alpha^2/KR)[(\Delta T/2) + T_C]}}{2R\alpha[(\Delta T/2) + T_C]}$$

OΓ

$$I = KR \Delta T \frac{1 + \sqrt{1 + z \left[ (\Delta T/2) + T_C \right]}}{R\alpha \left[ (\Delta T/2) + T_C \right]}$$

Because

$$\frac{\Delta T}{2} + T_C = \frac{T_h - T_C}{2} + T_C = \frac{T_h + T_C}{2}$$

we define the average temperature may be defined as:

$$\bar{T} = \frac{T_h + T_c}{2} \tag{33}$$

and

$$I = \frac{K\Delta T}{\alpha} \left\{ \frac{1 + \sqrt{1 + z \left[ (T_h + T_C)/2 \right]}}{(T_h + T_C)/2} \right\}$$
(34)

Multiplying equation (34) by

$$\frac{R\alpha}{R\alpha}\left(\frac{\sqrt{1+z\overline{T}}-1}{\sqrt{1+z\overline{T}}-1}\right)=1$$

and substitution of the average temperature given by equation (33) one obtains:

$$I = \frac{KR\alpha\Delta T}{R\alpha^2} \left\{ \frac{1 + \sqrt{1 + z\bar{T}}}{\bar{T}} \right\} \left( \frac{\sqrt{1 + z\bar{T}} - 1}{\sqrt{1 + z\bar{T}} - 1} \right)$$

With  $1/z = KR/\alpha^2$ , expansion gives:

$$I = \frac{\alpha \Delta T}{R} \left( \frac{z\bar{T}}{z\bar{T}\sqrt{1+z\bar{T}}-1} \right)$$

Rearranging yields the expression for the current that optimizes the coefficient of performance:

$$I_O = \frac{\alpha \Delta T}{R\left(\sqrt{1+z\overline{T}}-1\right)} \tag{35}$$

Figure 5 is a plot of the coefficient of performance as a function of current based on the conditions specified in equations (11) through (16).

#### 3. Optimum Coefficient Of Performance

Substituting  $I_0$  into the coefficient of performance equation (35) yields the optimum coefficient of performance:

$$\eta_O = \frac{T_C}{\Delta T} \left[ \frac{\sqrt{1+z\bar{T}} - \frac{T_h}{T_C}}{\sqrt{1+z\bar{T}} + 1} \right]$$
 (36)

As z approaches  $\infty$ ,  $\eta_O$  approaches the ideal, or Carnot, coefficient of performance which is the term to the left of the brackets in equation (36) Egli [Ref. 4: p. 31] and Tipler [Ref. 5:pp 575-576].

#### H. CASCADED COOLERS

If a large  $\Delta T$  is required, a multistage or cascaded cooler can be used. In a cascaded cooler the heat rejected by the first stage of couples is the heat load fed to the second stage. This arrangement can be extended to any number of stages. For best results when designing a multistage cooler for the lowest temperature attainable, each succeeding

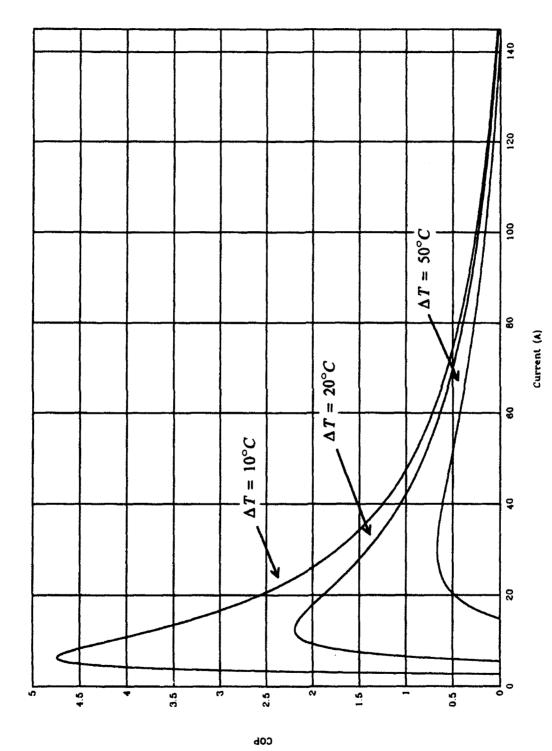


Figure 5 Coefficient of Performance as a Function of Current

stage should require less power than the previous stage. It is also possible to increase the coefficient of performance when the required temperature drop is close to the maximum for a given figure of merit Ioffe [Ref. 2: p. 116].

#### 1. Overall Heat Pumped By Cascaded Coolers

The heat pumped by a battery of n-stages of cascaded coolers is equal to the summation of the heat load,  $q_1$  at the first stage and the power required, P, of each stage over all stages in the battery:

$$q_{overall} = q_1 + \sum_{i=1}^{N} P_i$$
 (W)

#### 2. Overall Coefficient Of Performance

The coefficient of performance of a battery n-stages of cascaded coolers is the heat load of the first stage,  $q_1$ , divided by the total power required to operate the battery of coolers.

$$\eta_{overall} = \frac{q_1}{\sum_{i=1}^{N} P_i}$$

#### I. SUMMARY OF SIMPLIFYING ASSUMPTIONS

#### 1. Thomson Voltage

Neglect of the Thomson voltage results in no significant error. However, designs utilizing this model will be conservative, understating couple performance Kraus [Ref. 1: p. 322].

#### 2. Temperature Losses

Temperature losses between the thermoelectric couple and the heat load or heat exchanger are not taken into account directly. However, once determined, these temperature losses can be compensated for by adding the drop to the cold side temperature and subtracting the drop from the hot side temperature.

#### 3. Parallel Thermal Paths

Insulation between couples is assumed to be perfect, eliminating parallel thermal path heat losses.

#### 4. Junction Resistance

Junction resistance is assumed to be zero.

#### 5. Figure Of Merit

In order to maximize the figure of merit, the couple material lengths are assumed to be equal and area ratio determined by equation (25).

#### 6. Resistivity And Conductivity

Electrical resistivity, $\rho$ , and thermal conductivity, k, are assumed to be constant with respect to temperature.

#### 7. Couple Power Supply

The couple power supply is assumed to be direct current.

#### IV. THERMOELECTRIC COOLER DESIGN PROGRAM

#### A. INTRODUCTION

#### 1. Features

Thermoelectric Cooler Design is a Microsoft Windows program to be used as an aid in the design of thermoelectric cooler devices. Use of the Microsoft Windows graphical user interface allows the user who is familiar with the Windows environment to concentrate on the design process instead of a new, nonstandard interface. This program was written to be used to quickly model and compare alternative designs. Modifications to a design can be easily incorporated. Major features of the program include:

- 1. Ability to change material properties and dimensions of couples.
- 2. Determine optimum coefficient of performance of each couple.
- 3. Determine maximum heat pumping capacity of each couple.
- 4. The ability to analyze cascaded couples.
- 5. Graph the performance parameters of couple.
- 6. Provide on-line help in the form of a glossary, diagrams, and a temperature conversion calculator.

## 2. System Requirements

The minimum software and hardware requirements needed by the computer system to run Thermoelectric Cooler Design are:

- 1. Microsoft Windows, version 3.0 or later.
- 2. A hard drive with 500 kilobytes of free space.
- 3. A mouse that is supported by Windows.

#### 3. Disk Contents

Files included on the installation disk:

- 1. VBRUN100.DLL Visual Basic kernel which must be in the same directory as THERMAL.EXE.
- 2. THERMAL.EXE Thermolelectric Cooler Design executable file.
- 3. README.TXT This manual in ASCII format.

Both VBRUN100.DLL and THERMAL.EXE must be installed in order to run Thermoelectric Cooler Design.

#### 4. Installation

To install Thermoelectric Cooler Design:

- 1. Insert the installation disk in A: drive.
- 2. Exit to DOS. (Ensure C:\ prompt is present).
- 3. Type MD THERMAL then press the ENTER key.
- 4. Type COPY A:\\*.\* C:\THERMAL then press the enter key. These commands create a new directory named THERMAL on the C drive and

copy the files from the installation disk into the C:\THERMAL directory. However, this is only one of many different ways to copy the files from the installation disk to the computer. If the choice is to install Thermoelectric Cooler Design on another drive or in another directory, both VBRUN100.DLL and THERMAL.EXE must be installed together in the same directory. The program will not run if this is not the case.

- 5. Run Microsoft Windows.
- 6. Select the Program Manager.
- 7. Open the Group Window in which Thermoelectric Cooler Design is to be installed.
- 8. Choose the option "new" from the file menu of the Windows Program

  Manager window. The new program object dialog box will then appear.
- 9. Select the program item and choose OK. The program item properties dialog box appears.
- 10. Type a description to appear under the program icon.
- 11. Select the browse button to display a list of files and directories.
- 12. Select THERMAL.EXE and choose OK.
- 13. Select OK to close the program item properties dialog box.
- 14. The Thermoelectric Cooler Design program is now installed.

#### **B. USING THE PROGRAM**

# 1. Starting And Exiting The Program

To run Thermoelectric Cooler Design, simply double-click the program icon. After displaying the introduction, the program menu bar will appear. This program menu bar, titled "Thermoelectric Cooler Design" provides access to all program functions. To increase readability, select the minimize on use option under the Windows program manager options menu.

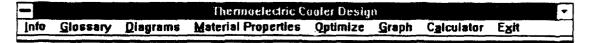


Figure 6 Program Menu Bar

To exit the program, select exit from the program menu bar and choose yes when prompted. Once exited, all current design data is lost.

# 2. Setting Material Properties

Prior to determining the optimum coefficient of performance or maximum heat pumping capacity of a couple, the material properties and dimensions of the couple must be input.

To begin, select material properties from the program menu bar. The material properties menu will appear with default values. If these values are acceptable, choose OK and proceed to the optimize menu. If the default values are not acceptable they may be changed by:

- Choosing either the first or second material. The α, ρ and k of the selected
  material is then displayed. All values in blue can be changed by the user.
  Appropriate values of α, ρ and k may be entered by the user by highlighting
  the text to be changed with the mouse and inputting the desired value from
  the keyboard.
- 2. Changes to the dimensions of the couple are input in a similar manner. Both the area and length of the second material may be input directly by the user.
- 3. Once the desired material properties and couple dimensions have been input, the overall resistance, thermal conductivity, and figure of merit are calculated by selecting the update button. In order to proceed to the optimize menu, select OK. To return all values to the defaults, choose the default button.

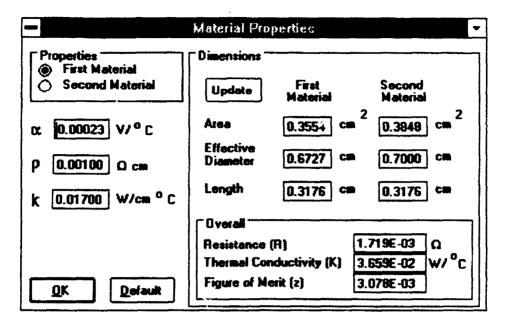


Figure 7 Material Properties Window

# 3. Optimum Coefficient Of Performance

To calculate the optimum coefficient of performance of a couple:

- 1. Ensure that the material properties menu has been reviewed.
- 2. Select the coefficient of performance option of the optimize menu.
- 3. The performance window will then appear. For a given low temperature the maximum high temperature is computed. The default  $\Delta T$  is the maximum and may be changed by manipulating the vertical scroll bar. Once the heat load, low temperature and  $\Delta T$  are acceptable, the optimum coefficient of performance is calculated by pressing the compute button. The optimum coefficient of performance and associated performance values are then displayed. Changes to the heat load, low temperature, and  $\Delta T$  can be made and all couple performance values recomputed by choosing restart.

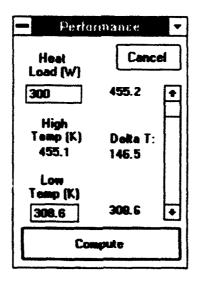


Figure 8 Optimum Coefficient of Performance Window

Optimum Coefficient of Performance						•
<u>Print</u>						
A/couple V/couple W/couple	23.37 n n569 1.33	qT 300.0 qP 3.1739 qJ 0.4636 qF 1.3941 qo 1.3102	W Total W Coeff	per of Couples Heat Rejected licient of Performance or Consumption	229 604 R 0.9843 304.8	w

Figure 9 Coefficient of Performance Results Window

# 4. Maximum Heat Pumping

To calculate the maximum heat pumping capacity of a couple:

- 1. Ensure that the material properties menu has been reviewed.
- 2. Select maximum the heat pumping option of the optimize menu.
- 3. The pumping window will appear. For a given low temperature the maximum high temperature is computed and displayed. The default temperature difference,  $\Delta T$ , is the maximum and may be changed by manipulating the vertical scroll bar. Once the heat load, low temperature, and  $\Delta T$  are acceptable, the maximum heat pumped is calculated by choosing compute. The maximum heat pumped and associated couple performance

values are then displayed. Changes to the heat load, low temperature and  $\Delta T$  can be made and all couple performance values recomputed by choosing restart.

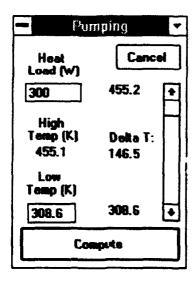


Figure 10 Maximum Heat Pumped Window

Print		Maximum l	leat Pumping	<b>-</b>
A/couple V/couple W/couple	78.99 0.1525 12.05	oP 10.7253 of 5.3626 of 1.3941	W Number of Couples W Total Heat Rejected W Coefficient of Performance W Power Consumption	76 1,215.8 0.3294 915.76

Figure Eleven Heat Pumped Results Window

# 5. Cascading Stages

Once the initial couple performance values have been computed for either optimum coefficient of performance or maximum heat pumping, cascading of multiple couple stages can be simulated by selecting cascade. The cascade button is not visible

until the first stage couple performance has been calculated. Each additional stage assumes the rejected heat of the previous stage at the heat load and the high temperature of the previous stage. The maximum temperature at the new low temperature is then calculated. While the  $\Delta T$  of the previous stage is assumed as a default, the  $\Delta T$  for every stage of the cascade can be changed with the vertical scroll bar. While the program only displays five stages at a time, an unlimited number of cascade stages can be computed and displayed. Results of stages beyond five are shown in either the optimum coefficient of performance or maximum heat pumping windows, but not in the cascade window.

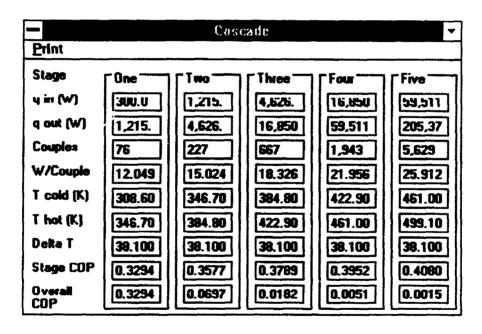


Figure Twelve Cascaded Stages Window

# 6. Graphing The Coefficient Of Performance And Heat Pumped

Thermoelectric Cooler Design is able to graph both coefficient of performance and heat pumped as a function of current. These graphs are useful in determining the

effect of a small change in current on both the maximum coefficient of performance and the heat pumped. The effects of varying the temperature differential across the couple can also be compared.

To graph either the coefficient of performance or heat pumped as a function of current:

- Ensure that the material properties have been reviewed and optimum coefficient of performance or maximum heat pumped has been determined.
   The graph option of the program menu bar will not be available until these steps are accomplished.
- 2. Select the graph option from the program menu bar. The graph window will appear.
- 3. Select the function option from the graph window menu bar. Choose either coefficient of performance versus current or heat pumped versus current.
- 4. Choose draw from the graph window menu bar. The selected function is then graphed for the temperature differential,  $\Delta T$ , chosen in the performance or heat pumped window.
- 5. To change the temperature differential, manipulate the  $\Delta T$  vertical scroll bar in either the performance or heat pumped window as appropriate.

To superimpose plots of representative of various temperature differentials and functions, select superimpose from under the options choice of the graph window menu bar. For example, to compare the effect of varying the temperature differential on a graph, change the  $\Delta T$  vertical scroll bar in either the performance or heat pumped window. Subsequent draw commands are then superimposed on the current graph. To clear the plot, deselect superimpose and then select draw

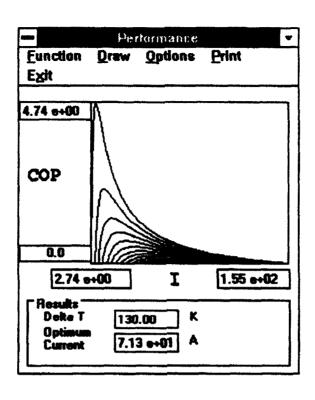


Figure Thirteen Optimum Coefficient of Performance Graph

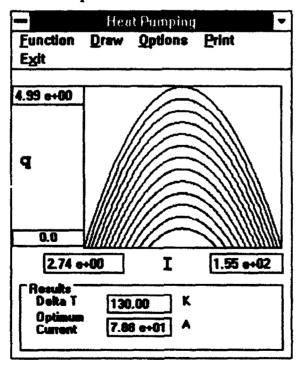


Figure Fourteen Maximum Heat Pumped Graph

The number of samples used to produce the graph may be adjusted as required.

Select the sample size desired under the samples choice under the options selection of the graph window menu bar.

# 7. Temperature Conversion Calculator

To convert between temperature scales:

- 1. Select the calculator option of the program menu bar. The temperature conversion calculator will appear.
- 2. Input the temperature to convert from by highlighting the blue numerical display with the mouse by holding down the left mouse button while sweeping the cursor from left to right across the calculator display text. Once the text is highlighted, type in the desired temperature.
- 3. Select the temperature scale to convert "from".
- 4. Select the temperature scale to convert "to".
- 5. Choose convert and read the temperature in the calculator display.
- 6. To clear the display, select clear display option.

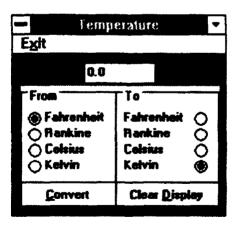


Figure Fifteen Temperature Conversion Calculator

# 8. Diagrams And Glossary

On-line assistance is available in the form of diagrams and a glossary.

Diagrams of a single couple and cascaded couples are available by selecting the diagram option from the program menu bar.

A glossary of terms used throughout the program is available. Choose the glossary option of the program menu bar.

#### V. CONCLUSIONS

The biggest drawback of a thermoelectric cooler is it's inherent low coefficient of performance, but new materials with better thermoelectric properties could eventually make thermoelectric devices competitive with compressor systems. While unable to compete directly with compressor based systems, thermoelectric coolers do have many unique characteristics making them useful in a variety of applications. For spaceborne applications, high reliability, vibration free operation, and no dependence on consumables are their most important features.

The design of thermoelectric coolers is tedious without the aid of a computer. Unfortunately, the utility of many programs written for DOS are handicapped by a poor user interface. More time is often required to figure out how to use the program than to solve the initial problem. In writing thermoelectric cooler design, the Windows graphical user interface was used to provide a better user interface. Windows offers the programmer several powerful program development tools. For the user, Windows offers a familiar working environment enabling the user to concentrate on the task at hand.

#### **APPENDIX**

Computer code listing for Thermoelectric Cooler Design program.

```
Thesis.txt
// Code for main menu bar
Sub ProgramInfoName_Click ()
  MsgBox "LCDR Clifton's Naval Postgraduate School Thesis"
End Sub
Sub DefinitionsName_Click()
  Definitions.Show
End Sub
Sub TemperatureName_Click()
  Screen.MousePointer = 11
  TempCalc.Show
  TempCalc.WindowState = 0
  Screen.MousePointer = 0
End Sub
Sub ChooseName_Click()
  Material.Show
End Sub
Sub ShowGraphName_Click()
  Screen.MousePointer = 11
  Graph.Show
  Graph. WindowState = 0
  Screen.MousePointer = 0
End Sub
Sub ExitName_Click()
  Screen.MousePointer = 11
  Ending.Show
  Screen.MousePointer = 0
End Sub
Sub Form_Load ()
  Main.Left = (Screen.Width - Main.Width) / 2
  Main.Top = 0
End Sub
```

```
Sub Form_Click ()
  Main.Left = (Screen.Width - Main.Width) / 2
  Main.Top = 0
End Sub
Sub PerformanceName_Click()
End Sub
Sub PumpingName_Click()
  Pumping.Show
End Sub
Sub Command1_Click()
  Results.CoeffText.Text = ""
  Results.NumberCouplesText.Text = ""
  Results.TotalHeatRejectedText.Text = ""
  Results.AperCoupleText.Text = ""
  Results. VperCoupleText.Text = ""
  Results.WperCoupleText.Text = ""
  Results.qTText.Text = ""
  Results.qPText.Text = ""
  Results.qJText.Text = ""
  Results.qFText.Text = ""
  Results.qoText.Text = ""
End Sub
Sub InfoName_Click ()
MsgBox "LCDR Clifton's Naval Postgraduate School Thesis"
End Sub
Sub SinglePumpingName_Click()
  Screen.MousePointer = 11
  ScrollUpdate = False
  Tc = Val(Pumping.LowTempText.Text)
  DeltaTMax = .5 * z * (Tc^2)
  TMax = DeltaTMax + Tc
  Pumping.Tempscroll.Max = Tc * 10 + 1
```

```
Pumping.Tempscroll.Min = TMax * 10 - 1
   Pumping.Tempscroll.Value = Pumping.Tempscroll.Min
   Pumping.TMinDisplay.Text = Format$(Tc. "##,##0.0")
   Pumping.TMaxDisplay.Text = Format$(DeltaTMax + Tc, "##,##0.0")
   Th = Pumping. Tempscroll. Value / 10
  Pumping.HighTempDisplay.Text = Format$(Th, "##,##0.0")
   DeltaT = Th - Tc
   Pumping.DeltaTDisplay.Text = Format$(DeltaT, "##,##0.0")
   Pumping.Show
  Pumping.WindowState = 0
  Screen. Mouse Pointer = 0
  ScrollUpdate = True
End Sub
Sub GlossaryName_Click()
  Screen, Mouse Pointer = 11
  Definitions. Show
  Definitions. Window State = 0
  Screen MousePointer = 0
End Sub
Sub CoolerName_Click()
  Screen.MousePointer = 11
  Cooler.Show
  Cooler.WindowState = 0
  Screen. Mouse Pointer = 0
End Sub
Sub CascadeName_Click()
  Screen.MousePointer = 11
  Cascade.Show
  Cascade. WindowState = 0
  Screen MousePointer = 0
End Sub
Sub SinglePerformanceName_Click()
  Screen.MousePointer = 11
```

```
ScrollUpdate = False
  Tc = Val(Performance.LowTempText.Text)
  DeltaTMax = .5 * z * (Tc^2)
  TMax = DeltaTMax + Tc
  Performance. Temps croll. Max = Tc * 10 + 1
  Performance. Tempscroll. Min = TMax * 10 - 1
  Performance.Tempscroll.Value = Performance.Tempscroll.Min
  Performance.TMinDisplay.Text = Format$(Tc, "##,##0.0")
  Performance.TMaxDisplay.Text = Format$(TMax, "##,##0.0")
  Th = Performance.Tempscroll.Value / 10
  Performance.HighTempDisplay.Text = Format$(Th, "##,##0.0")
  DeltaT = Th - Tc
  Performance.DeltaTDisplay.Text = Format$(DeltaT, "##,##0.0")
  Performance.Show
  Performance. WindowState = 0
  Screen.MousePointer = 0
  ScrollUpdate = True
End Sub
Sub MaterialName_Click()
  Screen.MousePointer = 11
  alpha_A = .00023
  alpha_B = .00021
  rho_A = .001!
  rho_B = .001!
  kappa_A = .017
  kappa_B = .0145
  Aa\_over\_Ab = Sqr((kappa\_B * rho\_A) / (kappa\_A * rho\_B))
  Ab = .3848
  Aa = Aa_{over}Ab * Ab
  dB = 2 * Sqr(Ab / pi)
  dA = 2 * Sqr(Aa/pi)
```

```
La = .318
  Lb = La
  alpha = alpha_A + alpha_B
  z = (alpha ^2) / ((Sqr(kappa_A * rho_A) + Sqr(kappa_B * rho_B)) ^2)
  R = (rho_A * La / Aa) + (rho_B * Lb / Ab)
  K = ((kappa_A * Aa) / La) + ((kappa_B * Ab) / Lb)
  Material.Option1.Value = True
  Material.AlphaText.Text = Format$(alpha_A, "0.00000")
  Material.RhoText.Text = FormatS(rho_A, "0.00000")
  Material.kText.Text = Format$(kappa_A, "0.00000")
  Material.FirstMaterial_a_Display.Text = FormatS(Aa, "##0.0000")
  Material.FirstMaterial_d_Display.Text = Format$(dA, "##0.0000")
  Material.SecondMaterial_d_Display.Text = Format$(dB, "##0.0000")
  Material.FirstMaterial_L_Display.Text = Format$(La, "##0.0000")
  Material.RDisplay.Text = Format$(R, "0.000E+00")
  Material.KDisplay.Text = Format$(K, "0.000E+00")
  Material.zDisplay.Text = Format$(z, "0.000E+00")
  Material.Show
  Material.WindowState = 0
  Screen.MousePointer = 0
End Sub
Material.txt
// Code for Material Properties Window
Dim Aa, Ab, La, Lb As Double
Sub Form_Load ()
  Material.Left = (Screen.Width - Material.Width) / 2
  Material.Top = (Screen.Height - Material.Height) / 2
End Sub
Sub Materials_Click()
End Sub
Sub Option1_Click()
  If Option 1. Value = True Then
```

```
AlphaText.Text = Format$(alpha A, "0.00000")
    RhoText.Text = Format$(rho_A, "0.00000")
    kText.Text = Format$(kappa_A, "0.00000")
  Else
    AlphaText.Text = Format$(alpha_B, "0.00000")
    RhoText.Text = Format$(rho_B, "0.00000")
    kText.Text = Format$(kappa_B, "0.00000")
  End If
End Sub
Sub Option2_Click()
  If Option 1. Value = True Then
    AlphaText.Text = Format$(alpha_A, "0.00000")
    RhoText.Text = Format$(rho_A, "0.00000")
    kText.Text = Format$(kappa_A, "0.00000")
  Else
    AlphaText.Text = Format$(alpha_B, '0.00000")
    RhoText.Text = Format$(rho_B, "0.00000")
    kText.Text = Format$(kappa_B, "0.00000")
  End If
End Sub
Sub AlphaText_Change ()
  If Option 1. Value = True Then
    alpha A = Val(AlphaText.Text)
  Else
    alpha_B = Val(AlphaText.Text)
  End If
End Sub
Sub RhoText_Change ()
  If Option 1. Value = True Then
    rho_A = Val(RhoText.Text)
  Else
    rho_B = Val(RhoText.Text)
  End If
End Sub
Sub kText_Change ()
  If Option 1. Value = True Then
    kappa_A = Val(kText.Text)
  Else
    kappa_B = Val(kText.Text)
```

```
End If
End Sub
Sub Command1_Click()
  Main.OptimizeName.Enabled = True
  Material.Hide
End Sub
Sub Command2_Click ()
  alpha_A = .00023
  alpha_B = .00021
  rho_A = .001!
  rho_B = .001!
  kappa_A = .017
  kappa_B = .0145
  Aa\_over\_Ab = Sqr((kappa\_B * rho\_A) / (kappa\_A * rho\_B))
  Ab = .3848
  Aa = Aa_over_Ab * Ab
  dB = 2 * Sqr(Ab/pi)
  dA = 2 * Sqr(Aa / pi)
  La = .318
  Lb = La
  alpha = alpha_A + alpha_B
  z = (alpha ^2) / ((Sqr(kappa_A * rho_A) + Sqr(kappa_B * rho_B)) ^2)
  R = (rho_A * La / Aa) + (rho_B * Lb / Ab)
  K = ((kappa_A * Aa) / La) + ((kappa_B * Ab) / Lb)
  Option 1. Value = True
  AlphaText.Text = Format$(alpha_A, "0.00000")
  RhoText.Text = Format$(rho_A, "0.00000")
  kText.Text = FormatS(kappa_A, "0.00000")
  FirstMaterial_a_Display.Text = Format$(Aa, "##0.0000")
  SecondMaterial_a_Display.Text = Format$(Ab, "##0.0000")
  FirstMaterial_d_Display.Text = Format$(dA, "##0.0000")
  SecondMaterial_d_Display.Text = Format$(dB, "##0.0000")
  FirstMaterial_L_Display.Text = Format$(La, "##0.0000")
  SecondMaterial_L_Display.Text = Format$(Lb, "##0.0000")
  RDisplay. Text = FormatS(R, "0.000E+00")
 KDisplay.Text = FormatS(K, "0.000E+00")
 zDispiay.Text = FormatS(z, "0.000E+00")
```

#### **End Sub**

```
Sub Command3_Click()
   Aa_over_Ab = Sqr((kappa_B * rho_A) / (kappa_A * rho_B))
   Ab = Val(SecondMaterial_a_Display.Text)
   Aa = Aa_over_Ab * Ab
   dB = 2 * Sqr(Ab / pi)
   dA = 2 * Sqr(Aa / pi)
  Lb = Val(SecondMaterial_L_Display.Text)
  La = Lb
  alpha = alpha_A + alpha_B
  z = (alpha ^ 2) / ((Sqr(kappa_A * rho_A) + Sqr(kappa_B * rho_B)) ^ 2)
  R = (rho_A * La / Aa) + (rho_B * Lb / Ab)
  K = ((kappa_A * Aa) / La) + ((kappa_B * Ab) / Lb)
  FirstMaterial_a_Display.Text = Format$(Aa, "##0.0000")
  SecondMaterial_a_Display.Text = Format$(Ab, "##0.0000")
  FirstMaterial_d_Display.Text = Format$(dA, "##0.0000")
  SecondMaterial_d_Display.Text = Format$(dB, "##0,0000")
  FirstMaterial_L_Display.Text = Format$(La, "##0.0000")
  SecondMaterial_L_Display.Text = Format$(Lb, "##0.0000")
  RDisplay. Text = Format$(R, "0.000E+00")
  KDisplay.Text = Format$(K, "0.000E+00")
  zDisplay.Text = FormatS(z, "0.000E+00")
End Sub
Coinput.txt
Sub Command1_Click()
  Screen.MousePointer = 11
  Stage = 0
  Performance.Hide
  History.Hide
  Results. Hide
  Screen.MousePointer = 0
End Sub
Sub Form_Load ()
  PerformanceCmd.Width = 2415
  Performance.Left = Screen.Width - Performance.Width
```

```
Performance.Top = Main.Height
  LowTempUpdate = True
  Cascading = False
End Sub
Sub Command2_Click ()
  Screen.MousePointer = 11
  Command2.Caption = "Wait"
  History. WindowState = 0
  LowTempUpdate = True
  Cascading = True
  Stage = Stage + 1
  If Stage = 1 Then
    TotalPower = 0
  End If
    Tc = Val(LowTempText.Text)
    Th = Val(HighTempDisplay.Text)
    DeltaT = Th - Tc
    Th_plus_Tc = Th + Tc
    gamma = Sqr(1 + (z/2) * (Th_plus_Tc))
    Io = (alpha * DeltaT) / (R * (gamma - 1))
    Vo = (alpha * DeltaT) + Io * R
    P = Io * Vo
    qT = Val(ReferLoadText.Text)
    qP = alpha * Io * Tc
    qJ = .5 * (Io ^2) * R
    qF = K * DeltaT
    qo = qP - (qJ + qF)
    No_of_Couples = qT/qo
    Total_Heat_rejected = qT + No_of_Couples * P
    Coeff_of_Performance = qo / P
    TotalPower = TotalPower + (P * No_of_Couples)
    If Stage = 1 Then
      FirstStage_qo = qo * No_of_Couples
    End If
    OverallCOP = FirstStage_qo / TotalPower
    TMaxDisplay.Text = Format$(DeltaTMax + Tc, "##,##0.0")
```

```
TMinDisplay.Text = Format$(Tc, "##,##0.0")
    DeltaTDisplay.Text = Format$(DeltaT, "##,##0.0")
    Results.CoeffText.Text = FormatS(Coeff_of_Performance, "0.0000")
    Results.NumberCouplesText.Text = Format$(No of Couples. "#,##0.00")
    Results.TotalHeatRejectedText.Text = Format$(Total_Heat_rejected, "#,##0.0")
    Results.AperCoupleText.Text = Format$(Io, "#,##0.00")
    Results. VperCoupleText.Text = Format$(Vo, "#,##0.0000")
    Results.WperCoupleText.Text = Format$(P, "#,##0.0000")
    Results.qTText.Text = FormatS(qT, "#,##0.0")
    Results.gPText.Text = Format$(qP, "#,##0.0000")
    Results.qJText.Text = Format$(qJ, "#,##0.0000")
    Results.gFText.Text = Format$(gF, "#,##0.0000")
    Results.qoText.Text = Format$(qo, "#,##0.0000")
    Results.Caption = "Optimum Coefficient of Performance" + " Stage " + Str$(Stage)
    Results.Show
    Select Case Stage
       Case 1
         History.qLoadStageOneDisplay.Text = Format$(qT, "#,##0.0")
         History.gRejectedStageOneDisplay.Text = FormatS(Total_Heat_rejected,
"#,##0.0")
         History.CouplesStageOneDisplay.Text = FormatS(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageOneDisplay. Text = Format$(P, "#,##0.0000")
         History.TcStageOneDisplay.Text = Format$(Tc, "0.0000")
         History. ThStageOneDisplay. Text = Format$(Th, "0.0000")
         History.DeltaTStageOneDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageOneDisplay.Text = FormatS(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageOneDisplay.Text = Format$(OverallCOP, "0.0000")
         History.Width = 2250
       Case 2
         History.qLoadStageTwoDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageTwoDisplay.Text = Format$(Total_Heat_rejected,
"#.##0.0")
         History.CouplesStageTwoDisplay.Text = Format$(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageTwoDisplay. Text = Format$(P, "#,##0.0000")
         History.TcStageTwoDisplay.Text = Format$(Tc, "0.0000")
         History. ThStageT woDisplay. Text = Format$(Th, "0.0000")
         History.DeltaTStageTwoDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageTwoDisplay.Text = Format$(Coeff_of_Performance,
"0.0000")
```

```
History.OverallCOPStageTwoDisplay.Text = Format$(OverallCOP, "0.0000")
         History.Width = 3360
       Case 3
          History.qLoadStageThreeDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageThreeDisplay.Text = Format$(Total_Heat_rejected,
"#,##0.0")
         History.CouplesStageThreeDisplay.Text = FormatS(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageThreeDisplay.Text = Format$(P, "#,##0.0000")
         History. TcStageThreeDisplay. Text = Format$(Tc. "0.0000")
         History. ThStageThreeDisplay. Text = Format$(Th. "0.0000")
         History.DeltaTStageThreeDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageThreeDisplay.Text = Format$(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageThreeDisplay.Text = Format$(OverallCOP,
"0.0000")
         History.Width = 4425
       Case 4
         History.qLoadStageFourDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageFourDisplay.Text = Format$(Total_Heat_rejected,
"#.##0.0")
         History.CouplesStageFourDisplay.Text = FormatS(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageFourDisplay. Text = Format$(P, "#,##0.0000")
         History.TcStageFourDisplay.Text = Format$(Tc, "0.0000")
         History. ThStageFourDisplay. Text = Format$(Th, "0.0000")
         History.DeltaTStageFourDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageFourDisplay.Text = FormatS(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageFourDisplay.Text = Format$(OverallCOP, "0.0000")
         History.Width = 5520
       Case 5
         History.qLoadStageFiveDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageFiveDisplay.Text = FormatS(Total_Heat_rejected,
"#,##0.0")
         History.CouplesStageFiveDisplay.Text = Format$(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageFiveDisplay. Text = Format$(P, "#,##0.0000")
         History.TcStageFiveDisplay.Text = Format$(Tc, "0.0000")
         History. ThStageFiveDisplay. Text = Format$(Th, "0.0000")
         History.DeltaTStageFiveDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageFiveDisplay.Text = FormatS(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageFiveDisplay.Text = Format$(OverallCOP, "0.0000")
```

```
History.Width = 6585
     End Select
     History.Show 0
     ScrollUpdate = False
     LowTempText.Text = Format$(Th, "##,##0.0")
     ScrollUpdate = True
     ReferLoadText.Text = Format$(Total_Heat_rejected, "##0.0")
     LowTempUpdate = False
     Tempscroli.Value = (Tc + DeltaT) * 10
     LowTempUpdate = True
     Command2.Caption = "Cascade"
     Screen.MousePointer = 0
     Cascading = False
End Sub
Sub TempScroll_Change ()
  If ScrollUpdate = True Then
    Tc = Val(LowTempText.Text)
    Th = Tempscroll. Value / 10
    DeltaT = Th - Tc
    HighTempDisplay.Text = Format$(Th, "##,#00.0")
    DeltaTDisplay.Text = Format$(DeltaT, "##,#00.0")
  End If
End Sub
Sub LowTempText_Change ()
If LowTempUpdate = True Then
  Tc = Val(LowTempText.Text)
  DeltaTMax = .5 * z * (Tc^2)
  TMax = DeitaTMax + Tc
 Tempscroll.Max = Tc * 10 + 1
  Tempscroll.Min = TMax * 10 - 1
 If Stage = 0 Then
    Tempscroll.Value = Tempscroll.Min
 End If
 Th = Tempscroll. Value / 10
```

```
If Cascading = False Then
     DeltaT = Th - Tc
  End If
  TMinDisplay.Text = Format$(Tc, "##,##0.0")
  TMaxDisplay.Text = Format$(TMax, "##,##0.0")
  DeltaTDisplay.Text = Format$(DeltaT, "##,##0.0")
End If
End Sub
Sub PerformanceCmd_Click()
  Screen.MousePointer = 11
  Main.ShowGraphName.Enabled = True
  PerformanceCmd.Caption = "Wait"
  Command2. Visible = -1
  History.Hide
  Stage = 0
    DeltaT = Th - Tc
    Th_plus_Tc = Th + Tc
    gamma = Sqr(1 + (z/2) * (Th_plus_Tc))
    Io = (alpha * DeltaT) / (R * (gamma - 1))
    Vo = (alpha * DeltaT) + Io * R
    P = Io * Vo
    qT = Val(ReferLoadText.Text)
    qP = alpha * Io * Tc
    qJ = .5 * (Io ^2) * R
    qF = K * DeltaT
    qo = qP - (qJ + qF)
    No_of_Couples = qT/qo
    Total_Heat_rejected = qT + No_of_Couples * P
    Coeff_of_Performance = qo / P
    TMaxDisplay.Text = Format$(DeltaTMax + Tc, "##,##0.0")
    TMinDisplay.Text = Format$(Tc, "##,##0.0")
    DeltaTDisplay.Text = Format$(DeltaT, "##,##0.0")
    Results.CoeffText.Text = Format$(Coeff_of_Performance, "0.0000")
    Results.NumberCouplesText.Text = Format$(No_of_Couples, "#,##0.00")
    Results.TotalHeatRejectedText.Text = Format$(Total_Heat_rejected, "#,##0.0")
    Results.AperCoupleText.Text = Format$(Io, "#,##0.00")
```

Results.VperCoupleText.Text = Format\$(Vo, "#,##0.0000")

Results. WperCoupleText.Text = Format\$(P, "#,##0.00")

Results.qTText.Text = Format\$(qT, "#,##0.0")

Results.qPText.Text = Format\$(qP, "#,##0.0000")

Results.qJText.Text = FormatS(qJ, "#,##0.0000")

Results.qFText.Text = Format\$(qF, "#,##0.0000")

Results.qoText.Text = Format\$(qo, "#,##0.0000")

Results.Caption = "Optimum Coefficient of Performance"

Results.Show

Results.PowerConsumptionDisplay.Text = Format\$((P \* No\_of\_Couples),

"#,###,##0.0")

PerformanceCmd.Width = 975

PerformanceCmd.Caption = "Restart"

Screen.MousePointer = 0

**End Sub** 

## Cooler.txt

// Code for Optimum Coeficient of Performance Window DefDbl A-Z

Global Const True = -1

Global Const False = 0

Global Const pi = 355 / 113

Global DeltaT As Double

Global DeltaTMax As Double

Global alpha\_A, alpha\_B, rho\_A, rho\_B, kappa\_A, kappa\_B As Double

Global alpha As Double

Global z, K, R As Double

Global Stage As Integer

Global ScrollUpdate As Integer

Global LowTempUpdate As Integer

Global Cascading As Integer

Global Total\_Heat\_rejected As Double

Global Tc As Double

Global Th As Double

Global TotalPower As Double

Global FirstStage\_qo As Double

#### Cascade.txt

// Code for Cascaded Stages Window

Sub PrintName\_Click ()

Cascade.PrintForm

```
End Sub
```

Sub ExitName\_Click ()
Cascade.Hide
End Sub

#### Define.txt

// Code to call Definitions Window Sub PrintName\_Click () Definitions.PrintForm End Sub

Sub ExitName\_Click ()
Definitions.Hide
End Sub

# Diagram.txt

// Code to call Diagrams
Sub PrintName\_Click ()
Cooler.PrintForm
End Sub

Sub ExitName\_Click ()
Cooler.Hide
End Sub

# Ending.txt

// Code to end design session, closing all open windows
Sub Command1\_Click ()
End
End Sub

Sub Command2\_Click ()
Ending.Hide
End Sub

Sub Form\_Click ()
Main.Left = (Screen.Width - Main.Width) / 2
Main.Top = (Screen.Height - Main.Height) / 2

End Sub

Sub Form\_Load ()

```
Ending.Left = (Screen.Width - Ending.Width) / 2
  Ending.Top = (Screen.Height - Ending.Height) / 2
End Sub
Graph.txt
// Code for graping routines
Dim Shown As Integer
Dim Samples As Integer
Dim IMax As Double
Dim IMin As Double
Dim YMax As Double
Dim YMin As Double
Dim OldYMax As Double
Dim OldIMax As Double
Dim OldIMin As Double
Dim OldMaxCount As Double
Dim OldMinCount As Double
Dim IatOldMinCount As Double
Dim IatOldMaxCount As Double
Dim PerformancePlot As Integer
Dim SuperimposePlots As Integer
Sub GraphIt ()
  ReDim I(Samples)
  ReDim Y(Samples)
  IMin = ((2 * alpha * Tc) - Sqr((2 * alpha * Tc) ^2 - (8 * R * K * DeltaT))) / (2 * R)
  IMax = ((2 * alpha * Tc) + Sqr((2 * alpha * Tc) ^ 2 - (8 * R * K * DeltaT))) / (2 * R)
  YMin = 0
  YMax = 0
  MinCount = 0
  MaxCount = 0
  Minimum = False
  StepInterval = (IMax - IMin) / (Samples - 1)
    If PerformancePlot = True Then
       YAxisLabel.Text = "COP"
```

Graph.Caption = "Performance"

Graph.Caption = "Heat Pumping"

YAxisLabel.Text = "q"

Else

```
End If
```

```
For J = 1 To Samples
             I(J) = IMin + StepInterval * (J - 1)
             If PerformancePlot = True Then
                   Y(J) = ((alpha * I(J) * Tc) - (.5 * I(J) ^ 2 * R) - (K * DeltaT)) / (I(J) * ((alpha * I(J) 
DeltaT) + (I(J) * R)))
             Else
                   Y(J) = (alpha * Tc * I(J)) - (.5 * I(J) ^ 2 * R) - (K * DeltaT)
             End If
             If Y(J) > 0 And Minimum = False Then
                   YMin = Y(J)
                   MinCount = J
                   Minimum = True
             ElseIf Y(J) > YMax Then
                   YMax = Y(J)
                   I_at_YMax = I(J)
             ElseIf Y(J) > 0 Then
                   MaxCount = J
            End If
            Next J
      If SuperimposePlots = True Then
             ResultsPicture.ScaleMode = 0
             ResultsPicture.ScaleTop = OldYMax
             ResultsPicture.ScaleHeight = -OldYMax
             ResultsPicture.ScaleLeft = IatOldMinCount
             ResultsPicture.ScaleWidth = IatOldMaxCount - IatOldMinCount
             YMaxText.Text = Format$(OldYMax, "0.00 e+00")
            IMinText.7 ext = Format$(OldIMin, "0.00 e+00")
            IMaxText.Text = Format$(OldIMax, "0.00 e+00")
      Else
             ResultsPicture.Cls
             ResultsPicture.ScaleMode = 0
             ResultsPicture.ScaleTop = YMax
             ResultsPicture.ScaleHeight = -YMax
             ResultsPicture.ScaleLeft = I(MinCount)
             ResultsPicture.ScaleWidth = I(MaxCount) - I(MinCount)
             YMaxText.Text = Format$(YMax, "0.00 e+00")
            IMinText.Text = Format$(IMin, "0.00 e+00")
            IMaxText.Text = Format$(IMax, "0.00 e+00")
```

```
OldYMax = YMax
    OldIMax = IMax
    OldIMin = IMin
    OldMaxCount = MaxCount
    IatOldMinCount = I(MinCount)
    IatOldMaxCount = I(MaxCount)
  End If
  For J = 1 To Samples
    ResultsPicture.Line (I(J-1), Y(J-1))-(I(J), Y(J))
  Next J
  I_at_YMaxDisplay.Text = Format$(I_at_YMax, "0.00 e+00")
  DeltaTDisplay.Text = Format$(DeltaT, "0.00")
End Sub
Sub ExitName_Click ()
  Graph.Hide
End Sub
Sub PrintName_Click()
  Graph.PrintForm
End Sub
Sub PerformanceName_Click()
  PerformancePlot = True
  PerformanceName.Checked = True
  PumpName.Checked = False
End Sub
Sub PumpName_Click()
  PerformancePlot = False
  PerformanceName.Checked = False
  PumpName.Checked = True
End Sub
Sub Form_Load ()
  PerformancePlot = True
  Samples = 200
End Sub
```

```
Sub DrawName_Click ()
  Screen.MousePointer = 11
  GraphIt
  SuperName.Enabled = True
  Screen. Mouse Pointer = 0
End Sub
Sub a100Name_Click()
  a100Name.Checked = True
  a200Name.Checked = False
  a500Name.Checked = False
  a1000Name.Checked = False
  Samples = 100
End Sub
Sub a200Name_Click()
  a100Name.Checked = False
  a200Name.Checked = True
  a500Name.Checked = False
  a1000Name.Checked = False
  Samples = 200
End Sub
Sub a500Name_Click()
  a100Name.Checked = False
  a200Name.Checked = False
  a500Name.Checked = True
  a1000Name.Checked = False
  Samples = 500
End Sub
Sub a 1000 Name Click ()
  a100Name.Checked = False
  a200Name.Checked = False
  a500Name.Checked = False
  a1000Name.Checked = True
  Samples = 1000
End Sub
Sub SuperName_Click ()
  If SuperName.Checked = False Then
```

```
SuperimposePlots = True
     SuperName.Checked = True
  Else
     SuperimposePlots = False
     SuperName.Checked = False
  End If
End Sub
History.txt
// Cascaded Stages Window menu bar
Sub Form_Load ()
  History.Left = 0
  History.Top = Main.Height
End Sub
Sub PrintName_Click()
  History.PrintForm
End Sub
Intro.txt
// Introduction graphic, program startup
Sub Timer1_Timer()
  Screen.MousePointer = 11
  Load Results
  Load Performance
  Load Material
  Load Definitions
  Load TempCalc
  Load Graph
  Load Cascade
  Main.Show
  Load Cooler
  Load Ending
  Load History
  Intro.Hide
  Timer 1. Enabled = 0
  Screen.MousePointer = 0
End Sub
Sub Form_Load ()
  Screen.MousePointer = 11
End Sub
```

```
Pumping.txt
// Code for Maximum Heat Pumped Window
Sub Command1_Click()
  Screen.MousePointer = 11
  Stage = 0
  Pumping.Hide
  History.Hide
  Results.Hide
  Screen.MousePointer = 0
End Sub
Sub Form_Load ()
  PerformanceCmd.Width = 2415
  Pumping.Left = Screen.Width - Pumping.Width
  Pumping. Top = Main. Height + 450
  LowTempUpdate = True
  Cascading = False
End Sub
Sub Command2_Click ()
  Screen.MousePointer = 11
  Command2.Caption = "Wait"
  History.WindowState = 0
  LowTempUpdate = True
  Cascading = True
  Stage = Stage + 1
  If Stage = 1 Then
    TotalPower = 0
  End If
    Tc = Val(LowTempText.Text)
    Th = Val(HighTempDisplay.Text)
    DeltaT = Th - Tc
    DeltaTMax = .5 * z * (Tc^2)
    Th_plus_Tc = Th + Tc
    gamma = Sqr(1 + (z/2) * (Th_plus_Tc))
    Io = (alpha * Tc) / R
```

```
Vo = alpha * Th
      P = Io * Vo
      qT = Val(ReferLoadText.Text)
      qP = alpha * Io * Tc
     qJ = .5 * (Io ^2) * R
     qF = K * DeltaT
     qo = .5 * ((alpha ^2 * Tc ^2) / R) - qF
     No\_of\_Couples = qT/qo
     Total_Heat_rejected = qT + No. of Couples * P
     Coeff_of_Performance = qo / P
     TotalPower = TotalPower + (P * No_of_Couples)
     If Stage = 1 Then
        FirstStage_qo = qo * No_of_Couples
     End If
     OverallCOP = FirstStage_qo / TotalPower
     TMaxDisplay.Text = Format$(DeltaTMax + Tc, "##,##0.0")
     TMinDisplay.Text = Format$(Tc, "##,##0.0")
     DeltaTDisplay.Text = Format$(DeltaT, "##,##0.0")
     Results.CoeffText.Text = Format$(Coeff_of_Performance, "0.0000")
     Results.NumberCouplesText.Text = Format$(No_of_Couples, "#,##0.00")
     Results.TotalHeatRejectedText.Text = Format$(Total_Heat_rejected, "#,##0.0")
     Results.AperCoupleText.Text = Format$(Io, "#,##0.00")
     Results. VperCoupleText.Text = Format$(Vo, "#,##0,0000")
     Results.WperCoupleText.Text = Format$(P, "#,##0.0000")
     Results.qTText.Text = Format$(qT, "#,##0.0")
     Results.qPText.Text = Format$(qP, "#,##0.0000")
     Results.qJText.Text = Format$(qJ, "#,##0.0000")
     Results.qFText.Text = Format$(qF, "#,##0.0000")
     Results.qoText.Text = Format$(qo, "#,##0.0000")
     Results. Caption = "Maximum Heat Pumping" + " Stage " + Str$(Stage)
     Results.Show
     Select Case Stage
       Case 1
         History.qLoadStageOneDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageOneDisplay.Text = Format$(Total_Heat_rejected,
"#,##0.0")
         History.CouplesStageOneDisplay.Text = Format$(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageOneDisplay. Text = Format$(P, "#,##0.0000")
         History.TcStageOneDisplay.Text = Format$(Tc, "0.0000")
         History. ThStageOneDisplay. Text = Format$(Th, "0.0000")
```

```
History.DeltaTStageOneDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageOneDisplay.Text = Format$(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageOneDisplay.Text = Format$(OverallCOP, "0.0000")
         History.Width = 2250
         History.qLoadStageTwoDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageTwoDisplay.Text = Format$(Total_Heat_rejected,
"#,##0.0")
         History.CouplesStageTwoDisplay.Text = Format$(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageTwoDisplay. Text = Format$(P, "#,##0.0000")
         History.TcStageTwoDisplay.Text = Format$(Tc, "0.0000")
         History.ThStageTwoDisplay.Text = Format$(Th, "0.0000")
         History.DeltaTStageTwoDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageTwoDisplay.Text = Format$(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageTwoDisplay.Text = Format$(OverallCOP, "0.0000")
         History.Width = 3360
       Case 3
         History.qLoadStageThreeDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageThreeDisplay.Text = Format$(Total_Heat_rejected,
"#,##0.0")
         History.CouplesStageThreeDisplay.Text = Format$(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageThreeDisplay. Text = Format$(P, "#,##0.0000")
         History.TcStageThreeDisplay.Text = Format$(Tc, "0.0000")
         History.ThStageThreeDisplay.Text = Format$(Th, "0.0000")
         History.DeltaTStageThreeDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageThreeDisplay.Text = Format$(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageThreeDisplay.Text = Format$(OverallCOP,
"0,0000")
         History. Width = 4425
       Case 4
         History.qLoadStageFourDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageFourDisplay.Text = Format$(Total_Heat_rejected,
"#,##0.0")
         History.CouplesStageFourDisplay.Text = Format$(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageFourDisplay. Text = Format$(P, "#,##0.0000")
         History. TcStageFourDisplay. Text = Format$(Tc, "0.0000")
         History. ThStageFourDisplay. Text = Format$(Th, "0.0000")
         History.DeltaTStageFourDisplay.Text = Format$(DeltaT, "0.0000")
```

```
History.StageCOPStageFourDisplay.Text = FormatS(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageFourDisplay.Text = Format$(OverallCOP, "0.0000")
         History.Width = 5520
       Case 5
         History.qLoadStageFiveDisplay.Text = Format$(qT, "#,##0.0")
         History.qRejectedStageFiveDisplay.Text = Format$(Total_Heat_rejected,
"#,##0.0")
         History.CouplesStageFiveDisplay.Text = FormatS(No_of_Couples,
"#,##0.00")
         History. WperCoupleStageFiveDisplay. Text = Format$(P, "#,##0.0000")
         History.TcStageFiveDisplay.Text = Format$(Tc, "0.0000")
         History. ThStageFiveDisplay. Text = Format$(Th, "0.0000")
         History.DeltaTStageFiveDisplay.Text = Format$(DeltaT, "0.0000")
         History.StageCOPStageFiveDisplay.Text = Format$(Coeff_of_Performance,
"0.0000")
         History.OverallCOPStageFiveDisplay.Text = Format$(OverallCOP, "0.0000")
         History.Width = 6585
    End Select
    History.Show 0
    ScrollUpdate = False
    LowTempText.Text = Format$(Th, "##,##0.0")
    ScrollUpdate = True
    ReferLoadText.Text = Format$(Total_Heat_rejected, "##0.00")
    LowTempUpdate = False
    Tempscroll. Value = (Tc + DeltaT) * 10
    LowTempUpdate = True
    Command2.Caption = "Cascade"
    Screen.MousePointer = 0
    Cascading = False
End Sub
Sub TempScroll_Change ()
  If ScrollUpdate = True Then
     Tc = Val(LowTempText.Text)
    Th = Tempscroll. Value / 10
     DeltaT = Th - Tc
     HighTempDisplay.Text = Format$(Th, "##,#00.0")
```

```
DeltaTDisplay.Text = Format$(DeltaT, "##,#00.0")
   End If
End Sub
Sub LowTempText_Change ()
If LowTempUpdate = True Then
  Tc = Val(LowTempText.Text)
  DeltaTMax = .5 * z * (Tc^2)
  TMax = DeltaTMax + Tc
  Tempscroll.Max = Tc * 10 + 1
  Tempscroll.Min = TMax * 10 - 1
  If Stage = 0 Then
     Tempscroll.Value = Tempscroll.Min
  End If
  Th = Tempscroll. Value / 10
  If Cascading = False Then
    DeltaT = Th - Tc
  End If
  TMinDisplay.Text = Format$(Tc, "##,##0.0")
  TMaxDisplay.Text = Format$(TMax, "##,##0.0")
  DeltaTDisplay.Text = Format$(DeltaT, "##,##0.0")
End If
End Sub
Sub PerformanceCmd_Click()
  Screen.MousePointer = 11
  Main.ShowGraphName.Enabled = True
  PerformanceCmd.Caption = "Wait"
  Command2. Visible = -1
  History.Hide
  Stage = 0
    DeltaT = Th - Tc
    Th_plus_Tc = Th + Tc
    gamma = Sqr(1 + (z/2) * (Th_plus_Tc))
    Io = (alpha * Tc) / R
    Vo = alpha * Th
```

```
P = Io * Vo
    qT = Val(ReferLoadText.Text)
    qP = alpha * Io * Tc
    qJ = .5 * (Io^2) * R
    qF = K * DeltaT
    qo = .5 * ((alpha ^2 * Tc ^2) / R) - qF
    No\_of\_Couples = qT/qo
    Total_Heat_rejected = qT + No_of_Couples * P
    Coeff_of_Performance = qo / P
     TMaxDisplay.Text = FormatS(DeltaTMax + Tc, "##,##0.0")
    TMinDisplay.Text = Format$(Tc, "##,##0.0")
    DeltaTDisplay.Text = Format$(DeltaT, "##,##0.0")
    Results.CoeffText.Text = Format$(Coeff_of_Performance, "0.0000")
    Results.NumberCouplesText.Text = Format$(No_of_Couples, "#.##0.00")
    Results.TotalHeatRejectedText.Text = Format$(Total_Heat_rejected, "#,##0.0")
    Results.AperCoupleText.Text = Format$(Io, "#,##0.00")
    Results. VperCoupleText. Text = Format$(Vo, "#,##0.0000")
    Results. WperCoupleText.Text = Format$(P, "#,##0.00")
    Results.qTText.Text = Format$(qT, "#,##0.0")
    Results.qPText.Text = Format$(qP, "#,##0.0000")
    Results.qJText.Text = Format$(qJ, "#,##0.0000")
    Results.qFText.Text = Format$(qF, "#,##0.0000")
    Results.qoText.Text = Format$(qo, "#,##0.0000")
    Results.Caption = "Maximum Heat Pumping"
    Results.Show
    Results.PowerConsumptionDisplay.Text = Format$((P * No_of_Couples),
"#,###,##0.00")
    PerformanceCmd.Width = 975
    PerformanceCmd.Caption = "Restart"
    Screen.MousePointer = 0
End Sub
Results.txt
// Code for Results Window
Sub Form_Click ()
  Results.Top = (Screen.Height - Results.Height)
  Results.Left = (Screen.Width - Results.Width) / 2
End Sub
```

```
Sub Form_Load ()
  Results.Top = (Screen.Height - Results.Height)
  Results.Left = (Screen.Width - Results.Width) / 2
End Sub
Sub PrintName_Click()
  Results.PrintForm
End Sub
Tempcalc.txt
// Code for Temperature Conversion Calculator
Sub Command2_Click()
  ConvertDisplayText.Text = ""
  ConvertDisplayText.SetFocus
End Sub
Sub ConvertCmd_Click()
  Const True = -1
  Const False = 0
  Temperature = Val(ConvertDisplayText.Text)
If FarenheitOutOption. Value = True Then
  If RankineInOption. Value = True Then
    Temperature = Temperature - 459.67
  ElseIf FarenheitInOption.Value = True Then
    Temperature = Temperature
  ElseIf CelsiusInOption. Value = True Then
    Temperature = (Temperature * 9 / 5) + 32
  ElseIf KelvinInOption. Value = True Then
    Temperature = ((Temperature - 273.15) * 9 / 5) + 32
  End If
ElseIf RankineOutOption.Value = True Then
  If RankineInOption. Value = True Then
    Temperature = Temperature
  ElseIf FarenheitInOption. Value = True Then
    Temperature = Temperature + 459.67
  ElseIf CelsiusInOption. Value = True Then
    Temperature = ((Temperature) * 9 / 5) + 32 + 459.67
  ElseIf KelvinInOption. Value = True Then
    Temperature = ((Temperature - 273.15) * 9 / 5) + 32 + 459.67
  End If
```

```
ElseIf CelsiusOutOption. Value = True Then
  If RankineInOption. Value = True Then
     Temperature = (Temperature - 32 - 459.67) * 5 / 9
  Elself FarenheitInOption. Value = True Then
     Temperature = (Temperature - 32) * 5 / 9
  ElseIf CelsiusInOption. Value = True Then
     Temperature = Temperature
  Elself KelvinInOption. Value = True Then
     Temperature = Temperature - 273.15
  End If
ElseIf KelvinOutOption.Value = True Then
  If RankineInOption. Value = True Then
     Temperature = (Temperature - 32 - 459.67) * 5 / 9 + 273.15
  ElseIf FarenheitInOption. Value = True Then
     Temperature = (Temperature - 32) * 5 / 9 + 273.15
  ElseIf CelsiusInOption. Value = True Then
     Temperature = Temperature + 273.15
  ElseIf KelvinInOption. Value = True Then
     Temperature = Temperature
  End If
End If
ConvertDisplayText.Text = Format$(Temperature, "##,##0.00")
ConvertDisplayText.SetFocus
End Sub
Sub Form_Click()
  ConvertDisplayText.SetFocus
End Sub
Sub Form_Load ()
  TempCalc.Left = (Sci ... Width - TempCalc.Width) / 2
  TempCalc.Top = (Screen.Height - TempCalc.Height) / 2
End Sub
Sub ExitName_Click()
  TempCalc.Hide
End Sub
```

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